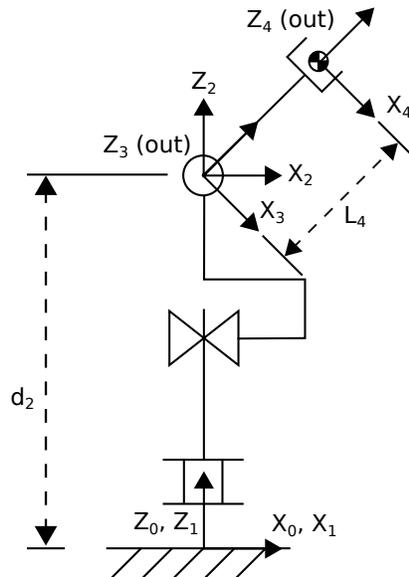


Make sure to provide justification for your answers. This includes labeling all of your plots (title, axes, legend, etc.) and explaining what is shown in the plots. Otherwise, you will lose points.

In this homework assignment, we will review kinematics and dynamics concepts from CS223A and then set up the simulation environment (SAI) that will be used for subsequent homework assignments and the final project.

1. Consider the RPR manipulator below. Assume this robot is massless except for the end effector, which is a point mass $m_4 = 1.0$ kg. Note that the joint angle θ_3 is negative in the configuration drawn below.



- (a) Find the position 0P_4 of the end effector expressed in frame $\{0\}$. *Hint:* Avoid DH parameters and use geometric intuition instead. Break up the projections by finding 2P_4 before 0P_4 .
- (b) Find the orientation 0R_4 of the end effector frame $\{4\}$ expressed in frame $\{0\}$. *Hint:* Break up the projections by finding 2R_4 before 0R_4 .
- (c) Find the linear Jacobian 0J_v of the end effector expressed in frame $\{0\}$.
- (d) Find the angular Jacobian ${}^0J_\omega$ of the end effector expressed in frame $\{0\}$.
- (e) Find the linear singularities of this robot. For each singularity you find, draw the robot in the singular configuration and specify the singular direction. Avoid taking the determinant and use intuition to identify the singularities.
- (f) Write out 0J_v for the singular configurations you drew above. For each configuration, explain why these are singularities in terms of joint motion. For each singular configuration, what is the singular direction expressed in frame $\{0\}$ when $\theta_1 = 0^\circ$? When $\theta_1 = 90^\circ$?
- (g) Find the joint space mass matrix M for this manipulator. Recall that all the robot is massless (i.e., no mass or inertia on any links or joints) except for the end effector, which is a point mass $m_4 = 1.0$ kg.
- (h) Find the gravity vector G . Assume acceleration due to gravity is $[0, 0, -g]^T$, where $g = 9.81 \text{ m s}^{-2}$.

